### 令和4年度第2次募集

## 新潟大学大学院自然科学研究科博士前期課程入学者選抜試験問題

Graduate School of Science and Technology, Niigata University

The Second Entrance Examination for the Master's Program

for Academic Year 2022

## 外国人留学生特別選抜

#### **Entrance Examination for International Students**

数理物質科学專攻 Major: Fundamental Sciences

数理科学 Course: Mathematical Science

A3

## 専門科目(数学) Specialized subjects (Mathematics)

#### 注意事項 Instructions

- 1. この問題冊子は、試験開始の合図があるまで開いてはいけません。 Do not open this booklet before the start of the examination is announced.
- 2. 問題冊子は、表紙を含めて全部で4ページあります。 This booklet consists of a total of 4 pages, including the cover page.
- 3. 試験時間は、 $9:00\sim11:00$  です。 The examination time is from 9:00 to 11:00.
- 4. 解答は、すべて解答用紙の指定された箇所に記入すること。 All answers must be written in the designated space on the Answer Sheets.
- 5. 受験番号は、各解答用紙の指定された箇所に必ず記入すること。 Your examinee's No. must be written in the designated space of each Answer Sheet.
- 6. 下書きは、問題冊子の余白を使用してください。 Please use a blank space of this booklet, if necessary.

# Problem 1

Find the eigenvalues and eigenvectors of the following matrix A.

$$A = \left(\begin{array}{rrr} 0 & 2 & -2 \\ 2 & 0 & 2 \\ -2 & 2 & 0 \end{array}\right)$$

# Problem 2

Consider the real-valued function

$$f(x,y) = 2x^2 - 2xy + 3y^2 - 4x - 8y.$$

Solve the following problems.

- (1) Calculate the partial derivatives  $\frac{\partial}{\partial x} f(x, y)$  and  $\frac{\partial}{\partial y} f(x, y)$ .
- (2) Give the Hessian matrix  $\nabla^2 f(x,y) = \begin{pmatrix} \frac{\partial^2}{\partial x^2} f(x,y) & \frac{\partial^2}{\partial y \partial x} f(x,y) \\ \frac{\partial^2}{\partial x \partial y} f(x,y) & \frac{\partial^2}{\partial y^2} f(x,y) \end{pmatrix}$ .
- (3) Locate all relative extrema of f.

# Problem 3

Write your research plan in the graduate school in English.